

# Qualitative deviation models vs. quantitative models for fault localization in spreadsheets

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# Spreadsheet Errors

Olympia 2012, London

~ 600 000 EUR damage



**JPMorganChase** 

~ 300 million EUR damage

# Spreadsheet Errors

Paper published by  
Reinhart & Rogoff

**HARVARD**  
UNIVERSITY



Many governments  
used it for decisions

Immense loss of  
reputation

	A	B	I	J	K	L	M
2			Real GDP growth				
3			Debt/GDP				
4	Country	Coverage	30 or less	30 to 60	60 to 90	90 or above	30 or less
26			3,7	3,0	3,5	1,7	5,5
27	Minimum		1,6	0,3	1,3	-1,8	0,8
28	Maximum		5,4	4,9	10,2	3,6	13,3
29							
30	US	1946-2009	n.a.	3,4	3,3	-2,0	n.a.
31	UK	1946-2009	n.a.	2,4	2,5	2,4	n.a.
32	Sweden	1946-2009	3,6	2,9	2,7	n.a.	6,3
33	Spain	1946-2009	1,5	3,4	4,2	n.a.	9,9
34	Portugal	1952-2009	4,8	2,5	0,3	n.a.	7,9
35	New Zealand	1948-2009	2,5	2,9	3,9	-7,9	2,6
36	Netherlands	1956-2009	4,1	2,7	1,1	n.a.	6,4
37	Norway	1947-2009	3,4	5,1	n.a.	n.a.	5,4
38	Japan	1946-2009	7,0	4,0	1,0	0,7	7,0
39	Italy	1951-2009	5,4	2,1	1,8	1,0	5,6
40	Ireland	1948-2009	4,4	4,5	4,0	2,4	2,9
41	Greece	1970-2009	4,0	0,3	2,7	2,9	13,3
42	Germany	1946-2009	3,9	0,9	n.a.	n.a.	3,2
43	France	1946-2022	4,9	2,7	3,0	n.a.	5,2
44	Finland	1946-2023	3,8	2,4	5,5	n.a.	7,0
45	Denmark	1946-2024	3,5	1,7	2,4	n.a.	5,6
46	Canada	1946-2025	1,9	3,6	4,1	n.a.	2,2
47	Belgium	1946-2026	n.a.	4,2	3,1	2,6	n.a.
48	Austria	1946-2027	5,2	3,3	-3,8	n.a.	5,7
49	Australia	1946-2028	3,2	4,9	4,0	n.a.	5,9
50							
51			4,1	2,8	2,8	=AVERAGE(L30:L44)	
52							

# Running Example

	A	B	C	D
1	Item	1st Qtr	2nd Qtr	Total
2	Units Sold	1000	1500	2500
3	ASP/Unit	\$ 20	\$ 21	\$ 20,6
4	Sales Revenue	\$ 20.000	\$ 31.500	\$ 51.500
5	Expenses	\$ 5.000	\$ 6.000	\$ 5.000
6	Operating Income	\$ 15.000	\$ 25.500	\$ 46.500
7	Op Income in %	75,0 %	81,0 %	90,3 %

= D4 / D2

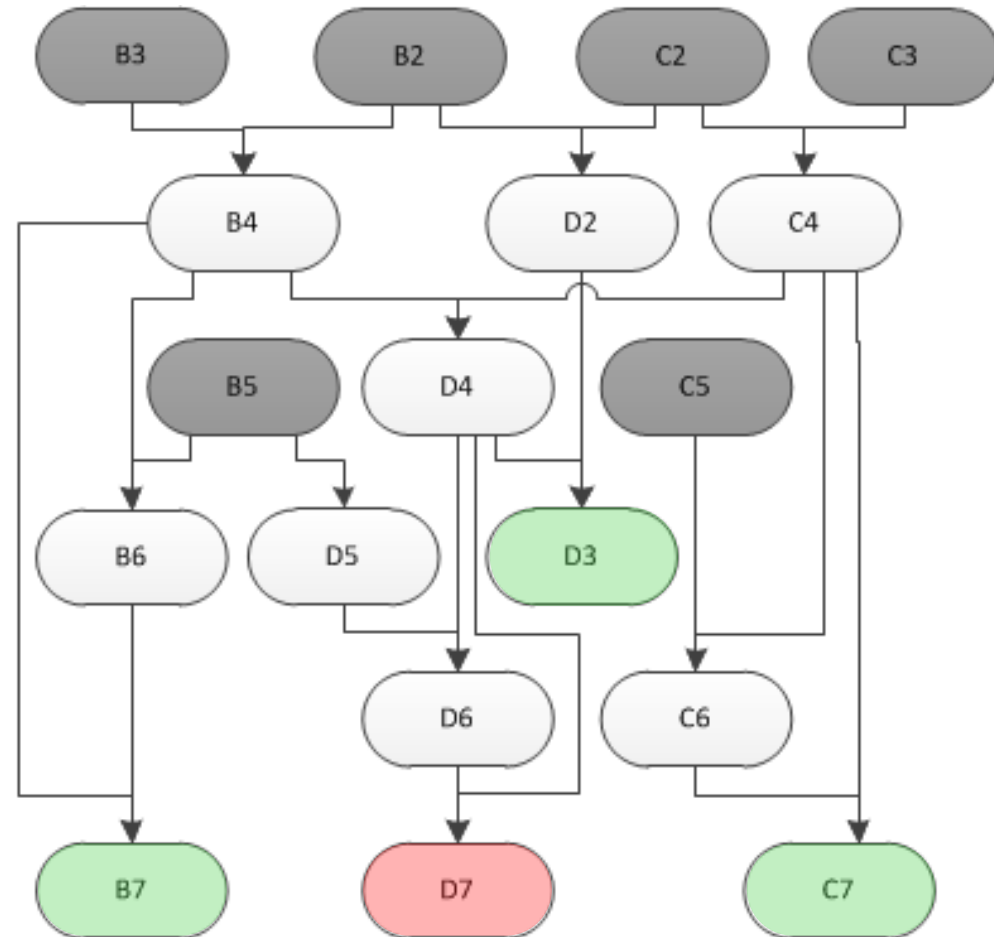
Should be  
78.6%

# Running Example – Formula View

	A	B	C	D
1	Item	1st Qtr	2nd Qtr	Total
2	Units Sold	1000	1500	=SUM(B2:C2)
3	ASP/Unit	20	21	=D4/D2
4	Sales Revenue	=B3*B2	=C3*C2	=SUM(B4:C4)
5	Expenses	5000	6000	=SUM(B5:B5)
6	Operating Income	=B4-B5	=C4-C5	=D4-D5
7	Op Income in %	=B6/B4	=C6/C4	=D6/D4

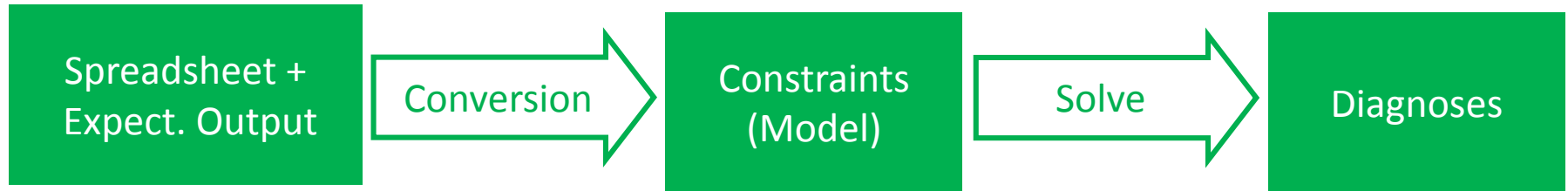
# Running Example – Dependency Graph

	A	B	C	D
1	Item	1st Qtr	2nd Qtr	Total
2	Units Sold	1000	1500	=SUM(B2:C2)
3	ASP/Unit	20	21	=D4/D2
4	Sales Revenue	=B3*B2	=C3*C2	=SUM(B4:C4)
5	Expenses	5000	6000	=SUM(B5:B5)
6	Operating Income	=B4-B5	=C4-C5	=D4-D5
7	Op Income in %	=B6/B4	=C6/C4	=D6/D4



This is a simplified version of the homework/Budgetone spreadsheet from the EUSES Spreadsheet Corpus

# Model-Based (Software) Debugging



	B	C	D
1	1st Qtr	2nd Qtr	Total
2	1000	1500	=SUM(B2:C2)
3	20	21	=D4/D2
4	=B3*B2	=C3*C2	=SUM(B4:C4)
5	5000	6000	=SUM(B5:B5)
6	=B4-B5	=C4-C5	=D4-D5
7	=B6/B4	=C6/C4	=D6/D4

Should be  
78,6%

AB(D2)  $\vee$  *behavior(D2)*  
 AB(D3)  $\vee$  *behavior(D3)*  
 AB(B4)  $\vee$  *behavior(B4)*

...

Test case:

D7 == 0,786

B7 == 0,750

...

For single faults:

SUM(AB(D2),AB(D3),...)==1

## Single Fault:

- {D5}
- {D6}
- {D7}

## Double Fault:

- {D3,D4}
- ...

All models are automatically derived from a faulty spreadsheet and also contain the fault!

# Models for a Spreadsheet's Behavior



## Value-based

$$D2 = B2 + C2$$

$$D3 = D4 / D2$$

## Dependency-based

$$\text{ok}(B2) \wedge \text{ok}(C2) \rightarrow \text{ok}(D2)$$

$$\text{ok}(D4) \wedge \text{ok}(D2) \rightarrow \text{ok}(D3)$$

	A	B	C	D
1	Item	1st Qtr	2nd Qtr	Total
2	Units Sold	1000	1500	=SUM(B2:C2)
3	ASP/Unit	20	21	=D4/D2
4	Sales Revenue	=B3*B2	=C3*C2	=SUM(B4:C4)
5	Expenses	5000	6000	=SUM(B5:B5)
6	Operating Income	=B4-B5	=C4-C5	=D4-D5
7	Op Income in %	=B6/B4	=C6/C4	=D6/D4



# Models for a Spreadsheet's Behavior



## Value-based

$$D2 = B2 + C2$$

$$D3 = D4 / D2$$

- + exact, few diagnoses
- computation time
- Reals: lacking support



## Dependency-based

$$\text{ok}(B2) \wedge \text{ok}(C2) \rightarrow \text{ok}(D2)$$

$$\text{ok}(D4) \wedge \text{ok}(D2) \rightarrow \text{ok}(D3)$$

- + fast
- + only Boolean
- many diagnoses

# Models for a Spreadsheet's Behavior

## Value-based

$$D2 = B2 + C2$$

$$D3 = D4 / D2$$

## Dependency-based

$$\text{ok}(B2) \wedge \text{ok}(C2) \rightarrow \text{ok}(D2)$$

$$\text{ok}(D4) \wedge \text{ok}(D2) \rightarrow \text{ok}(D3)$$

## Comparison-based

$$\text{eq}(B2) \wedge \text{eq}(C2) \rightarrow \text{eq}(D2)$$

$$\text{gt}(B2) \wedge \text{eq}(C2) \rightarrow \text{gt}(D2)$$

...

	A	B	C	D
1	Item	1st Qtr	2nd Qtr	Total
2	Units Sold	1000	1500	=SUM(B2:C2)
3	ASP/Unit	20	21	=D4/D2
4	Sales Revenue	=B3*B2	=C3*C2	=SUM(B4:C4)
5	Expenses	5000	6000	=SUM(B5:B5)
6	Operating Income	=B4-B5	=C4-C5	=D4-D5
7	Op Income in %	=B6/B4	=C6/C4	=D6/D4

# Comparison-based Modeling

$$\text{in1} + \text{in2} = \text{out}$$

$$\text{in1} * \text{in2} = \text{out}$$

ABNORMAL	in1	in2	out
False	=	=	=
False	<	=	<
False	=	<	<
False	<	<	<
False	>	=	>
False	=	>	>
False	>	>	>
False	<	>	?
False	>	<	?
True	?	?	?

$$\text{in1} - \text{in2} = \text{out}$$

$$\text{in1} / \text{in2} = \text{out}$$

ABNORMAL	in1	in2	out
False	=	=	=
False	<	=	<
False	=	<	>
False	<	<	?
False	>	=	>
False	=	>	<
False	>	>	?
False	<	>	<
False	>	<	>
True	?	?	?

# Practical Realization with Minion 1

```
1 MINION 3
2 # Modeling the domain = > <
3 # Values: 0 < / 1 = / 2 >
4
5 **VARIABLES**
6 DISCRETE Sheet1_F4{0..2}
7 DISCRETE Sheet1_F3{0..2}
8 DISCRETE tmp3{0..2}
9 DISCRETE Sheet1_H3{0..2}
10 DISCRETE Sheet1_B4{0..2}
11 DISCRETE Sheet1_D6{0..2}
12 DISCRETE Sheet1_B3{0..2}
13 DISCRETE Sheet1_D5{0..2}
14 DISCRETE Sheet1_D4{0..2}
15 DISCRETE Sheet1_D3{0..2}
16 DISCRETE Sheet1_F5{0..2}
17 DISCRETE tmp0{0..2}
18 DISCRETE Sheet1_B8{0..2}
19 DISCRETE Sheet1_B7{0..2}
20 DISCRETE Sheet1_B6{0..2}
21 DISCRETE Sheet1_B5{0..2}
22 DISCRETE tmp9{0..2}
23 BOOL ab[8]
24
25 **TUPLELIST**
26 plusMultFunction 40 4
27 0 1 1 1
28 0 2 1 2
29 0 1 2 2
30 0 2 2 2
31 0 0 1 0
32 0 1 0 0
33 0 0 0 0
34 0 0 2 0
35 0 0 2 1
36 0 0 2 2
37 0 2 0 0
38 0 2 0 1
39 1 0 0 0
40 1 0 0 1
41 1 0 0 2
42 1 1 0 0
43 1 1 0 1
44 1 1 0 2
45 1 2 0 0
46 1 2 0 1
47 1 2 0 2
48 1 0 1 0
49 1 0 1 1
50 1 0 1 2
51 1 0 2 0
52 1 0 2 1
53 1 0 2 2
54 1 1 1 0
67 minusDivFunction 40 4
68 0 1 1 1
69 0 2 1 2
70 0 1 2 0
71 0 2 2 0
72 0 2 2 1
73 0 2 2 2
74 0 0 1 0
75 0 1 0 2
76 0 0 0 0
77 0 0 0 1
78 0 0 0 2
79 0 0 2 0
80 0 2 0 2
81 1 0 0 0
82 1 0 0 1
83 1 0 0 2
84 1 1 0 0
85 1 1 0 1
86 1 1 0 2
87 1 2 0 0
88 1 2 0 1
89 1 2 0 2
90 1 0 1 0
91 1 0 1 1
92 1 0 1 2
93 1 0 2 0
94 1 0 2 1
95 1 0 2 2
96 1 1 1 0
```

# Practical Realization with Minion 2

```
123  **SEARCH**
124  VARORDER [ab]
125  PRINT [ab]
126
127  **CONSTRAINTS**
128  # System description
129  table([ab[4],Sheet1_D4,Sheet1_D5,Sheet1_F4], plusMultFunction)
130  table([ab[1],Sheet1_D3,Sheet1_D4,Sheet1_F3], plusMultFunction)
131  table([ab[3],Sheet1_B4,Sheet1_B6,Sheet1_D4], plusMultFunction)
132  table([ab[5],Sheet1_B7,Sheet1_B8,Sheet1_D5], plusMultFunction)
133  table([ab[6],Sheet1_D5,Sheet1_D6,Sheet1_F5], plusMultFunction)
134  table([ab[7],Sheet1_B8,Sheet1_B6,tmp9], plusMultFunction)
135  table([ab[0],Sheet1_B3,Sheet1_B4,tmp0], plusMultFunction)
136  table([ab[7],tmp9,Sheet1_B4,Sheet1_D6], plusMultFunction)
137  table([ab[2],Sheet1_F3,Sheet1_F4,tmp3], minusDivFunction)
138  table([ab[2],tmp3,Sheet1_F5,Sheet1_H3], minusDivFunction)
139  table([ab[0],tmp0,Sheet1_B5,Sheet1_D3], plusMultFunction)
140
141  # TEST CASE / Observations
142  eq(Sheet1_B8,1)
143  eq(Sheet1_B7,1)
144  eq(Sheet1_B6,1)
145  eq(Sheet1_H3,0)
146  eq(Sheet1_B3,1)
147  eq(Sheet1_B4,1)
148  eq(Sheet1_B5,1)
149
150  #SIZE OF SOLUTION
151  watchsumgeq(ab,1)
152  watchsumleq(ab,1)
153  **EOF**
```

# Empirical Evaluation

- 48 small spreadsheets (artificial + real life)
- Single, double, and triple faults
- Diagnostic accuracy
  - 24 spreadsheets: same diagnoses for all models
  - 20 spreadsheets : comparison- and dependency-based model same diagnoses
- Runtime

Model	Solving Time
Value-based	31 100 ms
Dependency-based	12 ms
Comparison-based	3 ms

# Summary and Conclusion

## Models for a Spreadsheet's Behavior

### Value-based

$$D2 = B2 + C2$$

$$D3 = D4 / D2$$

### Comparison-based

$$eq(B2) \wedge eq(C2) \rightarrow eq(D2)$$

$$gt(B2) \wedge eq(C2) \rightarrow gt(D2)$$

	A	...	B	C	
1	Item		1st Qtr	2nd Qtr	Total
2	Units Sold		1000	1500	=SUM(B2:C2)
3	ASP/Unit		20	21	=D2/B2
4	Sales Revenue		=B3*B2	=C3*C2	=SUM(D3:E3)
5	Expenses		5000	6000	=SUM(D4:E4)
6	Operating Income		=B4-B5	=C4-C5	=D4-D5
7	Op Income in %		=B6/B4	=C6/C4	=D6/D5

### Dependency-based

ok(B

ok(D

## Comparison-based Modeling

$$in1 + in2 = out$$

$$in1 * in2 = out$$

ABNORMAL	in1	in2	out
False	=	=	=
False	<	=	<
False	=	=	<
False	<	<	<
False	>	=	>
False	=	>	>
False	>	>	>
False	<	>	?
False	>	<	?
True	?	?	?

$$in1 - in2 = out$$

$$in1 / in2 = out$$

ABNORMAL	in1	in2	out
False			
False			
False			
False			
False			
False			
False			
False			
False			
True			

## Empirical Evaluation

- 48 small spreadsheets (artificial + real life)
- Single, double, and triple faults
- Diagnostic accuracy
  - 24 spreadsheets: same diagnoses for all models
  - 20 spreadsheets : comparison- and dependency-based model same diagnoses
- Runtime

Model	Solving Time
Value-based	31 100 ms
Dependency-based	12 ms
Comparison-based	3 ms

## Comparison-based model

- Short solving time
- Good diagnostic accuracy

→ Useful in practice